QUESTION Find $\frac{dy}{dx}$ at a general point on the curve $y^3 + xy + x^2 = 0$.

ANSWER

i.e.
$$\frac{dy}{dx}(3y^2 + x) = -(y + 2x)$$
, therefore $\frac{dy}{dx} + x\frac{dy}{dx} + y + 2x = 0$, $\frac{dy}{dx}(3y^2 + x) = -(y + 2x)$, therefore $\frac{dy}{dx} = -\frac{y + 2x}{3y^2 + x}$.