Vector Functions and Curves One variable functions

Question

Show that if the scalar product of the velocity and acceleration of an object in motion is negative (or positive) then the speed of the object is decreasing (or increasing).

Answer

$$\frac{d}{dt}|\underline{v}|^2 = \frac{d}{dt}\underline{v} \bullet \underline{v} = 2\underline{v} \bullet \underline{v}$$

Speed $v = |\underline{v}|$

If $\underline{v} \bullet \underline{a} > 0$ then the speed is increasing.

If $\underline{v} \bullet \underline{a} < 0$ then the speed is decreasing.