

Hypothesis Testing

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Learning Outcomes

Following this session you should be able to:

- Understand the concept and general procedure of hypothesis testing
- Understand the concept and interpretation of P values
- Explain the relationship between CI (point estimate ± 1.96 x S.E) & Hypothesis Testing
- Describe Type I & Type II Errors

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Hypothesis testing - milestones

- · Develop the research question
- Develop the research hypothesis
- State it as a statistical hypothesis
- Test the hypothesis
- · Was it a good idea?
- Next question(s)

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The Four Elements of a Research Question

- · Cells, Patient or Population
 - What or Who is the question about?
- Intervention or Exposure*
 - What is being done or what is happening to the cells, patients or population?
- Outcome(s)
 - How does the intervention affect the cells, patients or population?
- Comparison(s)
 - What could be done instead of the intervention
- *Intervention is intentional whereas an exposure is incidental

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Defining a Research Hypothesis

'A well-defined hypothesis crystallizes the research question and influences the statistical tests that will be used in analyzing the results'

http://intra.som.umass.edu/nakosteen/Topics/Developing%20the%20research%20design.doc [Accessed 17 Feb 2009]

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You cannot prove a hypothesis

- Falisifiability
 - (Karl Popper, 1902-1994)
- Scientific laws cannot be shown to be True or False
- They are held as Provisionally True
- · 'All Swans are White'
 - (David Hume, 1711-1776)



What is a Hypothesis?

- A tentative statement that proposes a possible explanation to some phenomenon or event
- A useful hypothesis is a **testable** statement which may include a prediction
- Any procedure you follow without a hypothesis is not an experiment

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Formalized Hypothesis

- IF and THEN
- · Specify a tentative relationship
- IF skin cancer is related to ultraviolet light, THEN people with a high exposure to UV light will have a higher frequency of skin cancer

Dependent variable

Independent variable



Disproving a hypothesis

- Collect evidence
- If evidence supports current hypothesis Hold hypothesis to be *Provisionally True*
- If evidence does not support hypothesis Reject hypothesis and develop new one
- · Statistical testing uses Null Hypothesis
 - No difference unless unlikely event (p)
 - Alternative hypothesis a difference?
 - Swans

Hypothesis	Testing
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Statistical Hypothesis testing -Overview

- · Define the problem
- State null hypothesis (H₀)
- State alternative hypothesis (H₁)
- Collect a sample of data to gather evidence
- · Calculate a test statistic

Test statistic = $\frac{\text{observed value - hypothesised value}}{\text{standard error of observed value}}$

- Relate test statistic to known distribution to obtain P value
- Interpret P value

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Defining the problem

- The null hypothesis assumes No Effect
 - $\mathbf{H}_{\mathbf{0}}$: There is no treatment effect in the population of interest
- The *alternative hypothesis* opposite of null hypothesis
 - $\mathbf{H_1}$: There is a treatment effect in the population of interest

Note: These are specified before collecting the data, they relate to the population not the sample and usually no direction is specified for the effect



Calculating the test statistic

The test statistic summarises the data from the sample in a single number. It's size indicates the amount of evidence gathered for either hypothesis

- The choice of test statistic will depend on the type of data collected and the hypotheses of interest
- 'Large' test statistic more evidence for H₁
- Values of the test statistic are standardized and can 'compare to published tables' – calculated

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How do we choose the test statistic?	
What is the measurement of interest? Means, proportions, etc	
What is the distribution of the measurement Normal or skewed	
 How many groups of patients are being studied? 1, 2, 3 or more 	
 Are they independent groups? or paired 	
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Interpretation of the P value	
The P value is the probability of getting a test statistic as large as, or larger than, the one obtained in the sample if the null hypothesis were true	
It is the probability that our results occurred by chance	
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Interpretation of the P value (2)	
• By convention, P values of <.05 are often accepted as "statistically significant" in the medical literature	

• It is an arbitrary cut-off

 A cut-off of P <.05 means that in about 5 out of 100 (1 in 20) experiments, a result would appear significant just by chance ("Type I error")

• We can use other P values for example 0.01



Interpretation of the P value (3)

- Large P value (usually > 0.05)
- Likely to have got results by chance if H₀ was true
 - Accept null hypothesis
 - Result is non-significant
- Small P value (usually < 0.05)
- Unlikely to have got results by chance if H_0 was true
 - Reject null hypothesis accept alternative hypothesis
 - Result is significant

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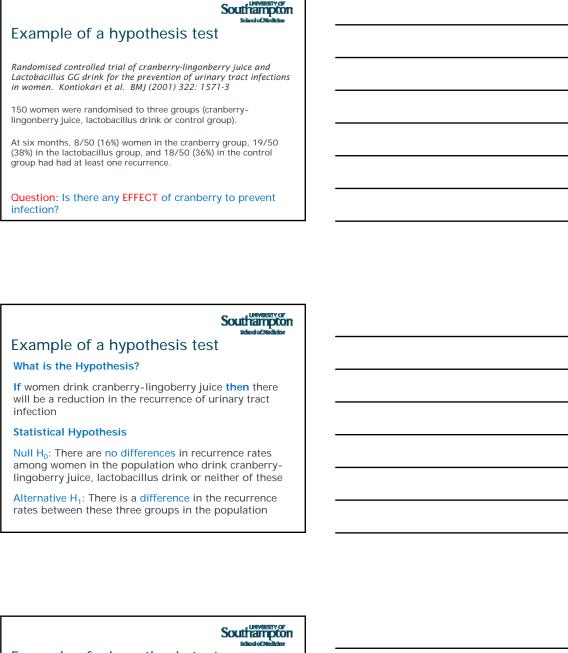
Where do P > 0.05 P > 0.01 P > 0.001 fit in?

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Adapted from Table 7 of White et al. (1979) with provincion of the audion; and publishes.									
	9.25	82	1.15	665	001	135	1,865	1301	6,005
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u	0.5	1.2	6.5	665	908	904	1.065	6.602	1,100
1	1.00	3.38	621	12.71	28.80	60	127.25	318.31	969
ż	9.82	1.30	2.52	430	5.95	230	1439	22.30	71.60
1	9.76	1.86	2.15	3.18	656	5.85	7.46	16.25	0.0
4	9.74	1.50	2.0	1.76	3.75	4.50	5.50	3.00	441
5	9.75	1.48	3.82	111	1.36	430	4.77	5.89	6.82
6									
ú.	9.79	1.37	1.81	133	2.76	327	3.58	4.14	4.99
m	9.29	1.76	1.00	130	2.72	101	3.50	440	644
u	2.20	130	1.00	4.70	600	3.85	3.30	140	444
14		1.34	1.76	114	2.62	2.86	3.33	1.79	4.14
ъ	9.50	134	1.75	1.0	2.60	2.95	3.29	1.79	4.01
ni .	9.50	134	1.75	1.0	2.50	2.30	325	1.65	468
O.		1.30	1.34	211	2.57	2.80	3.32	1.65	1.04
10	2.50	130	1.73	1.90	2.55	2.98	3.29	1.61	358
							1.10	3.58	1.88
30	2.60	130	1.02	109	2.59	2.84	1.95	155	185
21	2.65	1.30	1.02	100	2.52	2.80	3.14	131	1.02
13	1.50	132	1.72	2.04	2.58	2.82	12	1.90	3.79
23	1.68	130	1.71	100	2.50	2.80	1.16	1.41	XIT
34	1.00	132	1.71	2:06	2.49	2.88	1.65	140	3.34
25	1.58	1,32	t/H	106	2.48	2.79	1.68	1.61	3.11
Ni .	1.00	132	1.71	2:06	2.40	2.79	1.0	144	3.71
11	1.58	130	1.30	106	2.47	2.77	3.00	141	3.40
38	2.60	1.01	1.70	106	2.40	2.76	1.65	341	247
29	1.50	131	1.70	204	2.46	2.76	3.64	3.40	346
ю	1.68	130	1.10	104	2.46	2.79	1.01	1.10	140
40	LO	138	1.64	2.00	242	2.79	157	331	3.55
60	1.68	1.30	147	200	2.39	2.88	1.00	1.21	2.66
130	1.00	129	1.66	1.90	2.36	2.62	1.66	1.96	3.30
								1.09	5.29

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Example of a hypothesis test





Example of a hypothesis test

• Which test should be used?

Chi-squared test

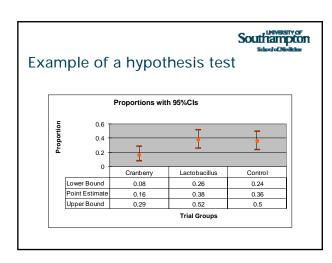
· What is the test statistic?

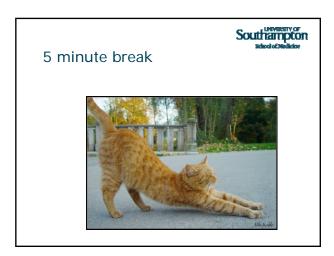
 X^2 7.05, P = 0.03

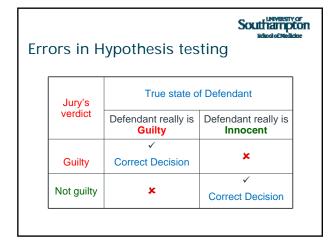
• How to interpret the result?

Reject null hypothesis

There is a significant difference in recurrence rates between these three groups (based on 5% significance)







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Types of Error in hypothesis testing

	True state of null h	ypothesis - Reality		
Statistical Decision	Null hypothesis is True	Null Hypothesis is False		
Accept	H ₀ accepted correctly	Type II error (β)		
Reject	Type I error (α)	H ₀ rejected correctly		

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Type I error

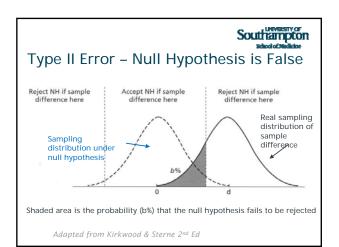
- The probability that we reject null hypothesis when it is true
- · 'False positive'
- ullet Rejected H_0 because the results occurred by chance
- Conclude that there is a significant effect, even though no true effect exists
- Probabilities of Type 1 error called alpha (α) Determined in advance, typically 5%

Type 1 Error – Null Hypothesis is True Reject NH if sample difference here Accept NH if sample difference here 2.5% Shaded areas gives the probability that the Null hypothesis is wrong rejected Adapted from Kirkwood & Sterne 2nd Ed



Type II error

- The probability that we accept null hypothesis when it is false
- · 'False Negative'
- Accept H₀ even though it is not true
- Conclude that there is no significant effect, even though a true difference exists
- Probabilities of Type II error called beta (β)



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Type II error rate

- Type II error rate depends on :
 - the size of the study
 - the variability of the measurement
- The implications of making either a type I or type II error will depend on the context of the study

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The Power of the Study	
The <i>power</i> of the study is the probability of correctly detecting a true effect	
Or the probability of correctly rejecting the null hypothesis	
Power = 100% - Type II error rate = (1 - β) x 100	
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3 ()	
 The power will be low if there are only a few observations 	
taking a larger sample will improve the power	
 The power will be low if there is variability amongst the observations 	
reducing variability will improve power	
 Ideally we would like a power of 100% but this is not feasible 	
usually accept a power of 80%	
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Things to consider

We can never be 100% certain that the correct decision has been reached when carrying out a hypothesis test

An hypothesis test cannot prove that a null hypothesis is true or false. It only gives an indication of the strength of evidence

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Questions	